St Teresa's Catholic Academy



'Our children are receptive, inquisitive learners who, through our Gospel values, have a unique sense of the world.'

Calculation Policy for Mathematics

September 2022

About our Calculation Policy

The following calculation policy has been devised to meet the requirements of the National Curriculum 2014 for the teaching and learning of mathematics. It is also designed to give pupils a consistent and smooth progression of learning in calculations across their primary mathematics learning. Please note the early learning in number and calculation in our Preschool and Foundation Stage follows the 'White Rose Scheme of Learning' document, and this calculation policy is designed to build on progressively from the content and methods established in the Early Years Foundation Stage. This calculation policy has been divided into concrete, pictorial and abstract (CPA) sections throughout. This is to ensure that CPA is use throughout the curriculum to support the children's learning.

Age Stage Expectations

This calculation policy is designed for a smooth transition from one method to the next, meaning that there is no definitive stage that each pupil should be at in relation to their year group. It is vital that pupils are taught according to the stage that they are currently working at, pupils will not be moved on to the next stage until they are secure in their understanding of the stage that is appropriate for their ability. In the National Curriculum 2014, it is expected that the majority of pupils will move through the programmes of study at 'broadly the same pace', with pupils who grasp concepts rapidly being challenged through rich and sophisticated tasks and challenges that deepen their understanding of concepts rather than moving them on to a new concept. Lower attaining children should be supported primarily through scaffolding and support through quality first teaching. This may also be supplemented with interventions.

Providing Context for Calculation: Problem Solving

It is imperative that any type of reasoning calculation is given a real-life context to help build children's understanding of the purpose of the calculation, and to help them recognise when to use certain operations and methods when faced with problems. This ensures that we meet the problem solving and reasoning aims set out in the National Curriculum 2014, whilst allowing the children to have a deeper understanding of the problems they are solving.

Addition						
EYFS:	Year 1:	Year 2:	Year 3:	Year 4:	Year 5:	Year 6:
Develop a deep understanding of the numbers to 10, the relationships between them and the patterns within those numbers.	Read, write and interpret mathematical statements involving addition (+) and equals (=) signs. Represent and use number bonds within 20. Add one-digit and two-digit numbers to 20, including zero. Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as 7 = ? + 3.	Recall and use addition facts to 20 fluently, and derive and use related facts up to 100. Add numbers using concrete, pictorial and abstract representations, including: -A two-digit number and ones. -A two-digit number and tens. -Two two-digit numbers. -Adding three one-digit numbers. To recognise and understand the inverse.	Add numbers mentally, including: -A three-digit. number and ones -A three-digit. number and tens -A three-digit number and hundreds. Add numbers with up to three digits, using formal written methods of columnar addition.	Add numbers with up to 4 digits using the formal written methods of columnar addition where appropriate.	Add whole numbers with more than 4 digits, including using formal written methods (columnar addition).	Add whole numbers with more than 4 digits, including using formal written methods (columnar addition).

Key Vocabulary:			STEM Sentences:				
Addend – A num	nber to be added	to another.		'One more than is'			
Aggregation – Combining two or more quantities or measures to find a total.			'I know that add is equal to ; therefore, add is equal to'				
Augmentation – Increasing a quantity or measure by another quantity.							
Commutative – 1	Numbers can be c	idded in any orde	ər.		·		
Complement – In addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000.		'We line ones. W ter	e up the ones; 'e line up the tens; s.' Etc.	ones add o ; tens add	nes equals tens equals		
Exchange – Change a number or expression for another of an equal value.			other of	'We know there are ten hundreds in one thousand, so hundred add hundred is equal to thousand			
Partitioning – Spl	itting a number int	o its component	parts.	hundred.'			
Subitise – Instant small group with	ly, recognising the out needing to co	number of objecture.	cts in a				
Subtrahend – A number to be subtracted from another.							
Sum – The result of an addition.							
Total – The aggre	egate or the sum f	ound by addition).				





Stage 3					
Add three 1-digit numbers					
	Example questions: $7 + 6 + 3 = 16$				
<u>Concrete:</u>	<u>Pictorial:</u>	<u>Abstract</u>			
	7+6+3=16	7+6+3=16 10			
	$\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 $	7 + 6 + 3 = 16 ? + 6 + 3 = 16			
When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add numbers more effectively. For children to truly embed this concept they need to see the pattern through concrete resources first. For example, seeing that the Numicon of 3 first together with the Numicon piece of 7 to form and Numicon 10 piece. Manipulatives that highlight number bonds to 10 are effective when adding three 1- digit numbers. This supports children in their understanding of commutativity.	When the children are using pictorial representations, they should us them in conjunction with the concrete initially. If possible, use pictorial representations that mirror the concrete resources. For example, if they have used tens frames in the concrete, then they should be drawing (or looking at) tens frames during the pictorial. Then they should be moving on to new questions with different pictorial representations.	At this stage, as with the concrete and pictorial, the children should be looking for their number bonds to 10. If they cannot identify them then they need to go back to the concrete so that they can visually see the importance of number bonds. If the children are not using their number bonds, it is important to stop them and make it explicit for them. This is a key concept that should not be missed or overlooked.			







Stage 7						
	Add numbers with up to 4 digits					
	Example questions: 1,378 + 2,148 = 3,526					
	Pictorial:	Abstract: $ \begin{array}{r} 1 & 3 & 7 & 8 \\ + & 2 & 1 & 4 & 8 \\ \hline 3 & 5 & 2 & 6 \\ \hline 1 & 1 \\ \end{array} $ 1,378 + 2,148 = 3,526				
Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 4 digits. Ensure children write out their calculations alongside any concrete resources, so they can see the links to the written method, or that the abstract is visible to them somewhere. Plain counters on a place value grid can also be used to support learning. This is where it needs to be made explicit to the children that, as when there are 10 ones, we exchange 1 ten, when there are 10 tens, we exchange 1 hundred and so on	If the children have used base 10 resources as their concrete manipulatives, then they should use base 10 as their pictorial. Base 10 and place value counters are key to the children understanding exchanging. They should be using the concrete alongside the pictorial – or the digital tools on the White Rose website.	Ensure children write out their calculations alongside any concrete and pictorial resources so they can see the links to the written column method. This supports their understanding of exchanging when they are completing abstract calculations. When exchanging, the children need to put the exchanged digit underneath the formal column written method. To ensure a deep understanding, the children should be confident and competent doing missing number problems and understand that the equals sign can go on either side of the calculation.				

Stage 8				
	Add numbers with more than 4 digits			
Ex	ample question: 104,328 + 61,731 = 166,0)59		
<u>Concrete:</u>	<u>Pictorial:</u>	Abstract:		
HTh TTh Th H T O	? 104,528 61/31	104,328 + 61,731 = 166,059		
	104,328 61,731 61731 ?	1 0 4 3 2 8		
		+ 6 1 7 3 1		
		1 6 6 0 5 9		
		1		
		104,328 + = 166,059		
Place value counters or plain counters on a place value grid are the most effective concrete resources when adding numbers with more than 4 digits. At this stage, place value counters can be used to both support the learning as well as extend it. Higher ability children often find it had to demonstrate mathematical concepts accurately when using concrete resources. Again, it needs to be made explicit to the children that, as when there is 10 ones, we exchange 1 ten, when there is 10 tens, we exchange 1 hundred and so on	Using bar models and part-whole models can help children to understand that calculations work in a number of ways, e.g. the inverse. They can also support the children's understanding of the value of numbers - bigger numbers will have a bigger section of the bar model. Drawing out place value counters are a good step for demonstrating that the children truly understand how exchanging works.	At this stage, children should be encouraged to work in the abstract, using the column method to add larger numbers effectively. When exchanging, the children need to put the exchanged digit underneath the formal column written method. To ensure a deep understanding, the children should be confident and competent doing missing number problems and understand that the equals sign can go on either side of the calculation. They should also understand the inverse.		



Subtraction						
EYFS:	Year 1:	Year 2:	Year 3:	Year 4:	Year 5:	Year 6:
Develop a deep understanding of the numbers to 10, the relationships between them and the patterns within those numbers.	Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs. Represent and use number bonds and related subtraction facts within 20. Subtract one-digit and two-digit numbers to 20, including zero. Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = ? – 9.	Recall and use subtraction facts to 20 fluently and derive and use related facts up to 100. Subtract numbers using concrete, pictorial and abstract representations, including: -A two-digit number and ones. -A two-digit number and tens. -Two two-digit numbers. To recognise and understand the inverse.	Subtract numbers including: -A three-digit. number and ones -A three-digit. number and tens -A three-digit number and hundreds. Subtract numbers with up to three digits, using formal written methods of columnar subtraction.	Subtract numbers with up to 4 digits using the formal written methods of columnar subtraction where appropriate.	Subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction).	Subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction).
Key Vocabu	lary:		STEM	Sentences:		

Difference – The numerical difference between two numbers is found by comparing the quantity in each	'One less than is'			
group. Exchange – Change a number or expression for another of an equal value.	'I know that subtract is equal to ; therefore, subtract is equal to'			
Minuend – A quantity or number from which another is subtracted.	' subtract is equal to'			
Partitioning – Splitting a number into its component parts.	'We line up the ones; ones subtract ones equals ones. We line up the tens; tens subtract tens			
Subitise – Instantly, recognising the number of objects in a	equais iens. eic.			
small group without needing to count.	'We know there are ten hundreds in one thousand, so hundred subtract hundred is equal to thousand			
Subtrahend – A number to be subtracted from another.	hundred.'			
Stage 1				
Subtract 1-digit numbers within 10				

Example question: 7 – 3 = 4					
Concrete:	Pictorial: 1 2 3 4 5 6 7 8 9 10 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	$\frac{\text{Abstract:}}{7-3=4}$			
Cubes and tens frames are excellent concrete resources to demonstrate reduction. Cubes or counters can be physically taken away from the amount. Ten frames, cubes, and bead strings support reduction.	Bar models should be used in conjunction with the concrete representations. The pictorial bar model is almost exactly the same and the cubes (concrete). Number lines can support children's understanding of counting backwards - reduction. Part-whole models, bar models, ten frames and number shapes support partitioning.	The abstract calculation should be shown alongside the concrete resource so that the children can clearly see the relationship been the abstract and the concrete.			
Stage 2					
Subtract 1 and 2-digit numbers within 20					
Example questions: 14 – 6 = 8					

Concrete:	Pictorial:	Abstract:		
		14 - 6 = 8		
		14 - 6 = 8		
	1 2 3 4 5 6 7 9 10 11 12 13 16 15 16 17 18 19 20	4 2		
When subtracting 1-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten. Children should be encouraged to find the number bond to 10 when partitioning the subtracted number. Tens frames, cubes, base 10 and number lines are particularly useful for this.	Counting back on number lines help support the children's understanding of subtraction – reduction. Again, children should be looking for number bonds again. They should be looking for the amount to subtract to reach the previous multiple of 10.	The abstract calculation should be shown alongside the concrete resource so that the children can clearly see the relationship been the abstract and the concrete.		
	Bar models and part-whole models support the children's understanding of partitioning. This also helps them to see the relationship between addition and subtraction.			
Stage 3				
	Subtract 1 and 2-digit numbers to 100			
Example questions: 65 – 28 = 37				

Concrete:	Pictorial:	Abstract:		
	65 (65 (28) (28	65 - 28 = 37		
Tens Ones IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII		- 28 37		
At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 and place value counters. As numbers become larger, straws become less effective.	Exchanging from another column is a hard concept for children to understand; therefore, they should use pictorial representations alongside the concrete at this point to secure their understanding. The abstract should also be visible.	At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 and place value counters. When completing the formal written method, the children should be placing		
Even when using concrete resources, it should be made explicit to the children that they should start by taking away the ones and then move to the left. This is where the children need to understand that 1 ten equals 10 ones. This exchanging must be modelled clearly to the children.	Bar models and part-whole models support the children's understanding of partitioning. This also helps them to see the relationship between addition and subtraction.	the exchanged number at the top left of the original digit – as seen above. IT should be made clear that they need to start from the ones column and then move to the left though the remaining columns.		
Stage 4				
Subtract numbers with up to 3 digits				
Example questions: 435 – 273 = 262				

Concrete:	<u>Pictorial:</u>	Abstract:		
Hundreds Tens Ones Image: State of the	HundredsTensOnesImage: state st	$435 - 273 = 262$ $\begin{array}{r} {}^{3}4^{1}35 \\ - 273 \\ \hline 262 \end{array}$		
Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits. Plain counters on a place value grid can also be used to support learning. Ensure children write out their calculations alongside any concrete resources so they can see the links to the formal written method.	Alongside the concrete and abstract, the children should be drawing out the pictorial. Bar models and part-whole models support the children's understanding of partitioning. This also helps them to see the relationship between addition and subtraction.	When completing the formal written method, the children should be placing the exchanged number at the top left of the original digit – as seen above. The children should be reminded that the start from the ones column and then move to the left though the remaining columns.		
Stage 5				
Subtract numbers with up to 4 digits				
Example questions: 4,357 – 2,735 = 1,622				

Concrete:	Pictorial:	Abstract:		
Thousands Hundreds Tens Ones I I I IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	Thousands Hundreds Tens Ones Items Items Items Items Items Items <t< td=""><td>4,357 - 2,735 = 1,622 $4,357 - 2,735 = 1,622$ $- 2735 = 1,622$</td></t<>	4,357 - 2,735 = 1,622 $4,357 - 2,735 = 1,622$ $- 2735 = 1,622$		
Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 4 digits. Plain counters on a place value grid can also be used to support learning. Ensure children write out their calculations alongside any concrete resources so they can see the links to the formal written method.	Alongside the concrete and abstract, the children should be drawing out the pictorial. Bar models and part-whole models support the children's understanding of partitioning. This also helps them to see the relationship between addition and subtraction.	When completing the formal written method, the children should be placing the exchanged number at the top left of the original digit – as seen above. The children should be reminded to start from the ones column and then move to the left though the remaining columns.		
Stage 6				
Subtract numbers with more than 4 digits				
Example questions: 294,382 – 182,501 = 111,881				

Concrete:	Pictorial:	Abstract:								
HTh TTh Th H T O	HTh TTh Th H T O	294,382 - 182,501 = 111,881								
			2	9	³ /	¹ 3	8	2		
	294,382 294,382 1 182,501 ?	-	1	8	2	5	0	1		
	(182,501) ? 182,501 ? 182,501 ?		1	1	1	8	8	1		
Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.	Bar models and part-whole models support the children's understanding of partitioning. This also helps them to see the relationship between addition and subtraction.	At the encour colum number When metho the ex the or childred from the the lef	nis st ragec n m ers effi com d, the chan chan chan t thou	age, to we ethoc cientl pletin e child ged n digit uld be es co gh the	child ork in 1 to y. umbe – as e remi lumn e remo	dren the a sub e fo should r at th seen nded and t aining	shou bstract tract rmal d be ne top abo that t hen n colur	uld be ct, using larger written placing o left of ve. The the start nove to mns.		
	Stage 7									
	Subtract with up to 3 decimal places									

<u>Concrete:</u>	Pictorial: Over Texts Hurdeeths	Abstract:
Ones Tenths Hundredths 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1<	2.7 5.43 5.43 2.7 2.7 2.7 2.7 2.7 2.7 2.7 2.7	$5.43 - 2.7 = 2.73$ $\begin{array}{r}4^{4} \\ 5.43 \\ -2.7 \\ \hline 2.73\end{array}$
Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 or 3 decimal places. Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this in context when subtracting money and other measures that can be used as a concrete resource.	Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this in context when subtracting money and other measures that can be used as a pictorial resource.	When completing the formal written method, the children should be placing the exchanged number at the top left of the original digit – as seen above. The children should be reminded that the start from the furthest column on the right (dependent on the number of decimal places) and then move to the left through the remaining columns. It should be made clear to the children that they need to put the decimal point in their answer before they start working out – to avoid errors.

Multiplication								
EYFS:	Year 1:	Year 2:	Year 3:	Year 4:	Year 5:	Year 6:		

Doubling, sharing and grouping.	Solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.	Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers. Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (×) and equals (=). Show that multiplication of two numbers can be done in any order (commutative).	Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables. Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.	Recall multiplication facts for tables up to 12 × 12. Multiply mentally, including multiplying by 0 and 1 and multiplying together three numbers. Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.	Identify and understand multiples and factors; square numbers and cube numbers; prime numbers and composite (nonprime) numbers. Multiply numbers up to 4 digits by a 1-digit and 2-digit numbers using the formal written method of short division, long division and interpret remainders. Multiply whole numbers by 10, 100 and 1000.	Multiply multi-digit numbers up to 4 digits by a two- digit whole number using the formal written method of long multiplication. Identify common factors, common multiples and prime numbers.
------------------------------------	---	---	--	---	--	--

Key Vocabulary:	STEM Sentences:
	'There are apples; the total value is'

 Array – An ordered collection of counters, cubes or other item in rows and columns. Commutative – Number can be multiplied in any order. 	'There are coins. Each coin has a value of p. This is p.'						
Exchange – Change a number or expression for another of an equal value.	each group. There are groups of'						
Factor – A number that multiplies with another to make product.	and						
Multiplicand – In multiplication, a number to be multiplied by another.	tenths is equal to tenths.'						
Partitioning – Splitting a number into its component parts.							
Product – The result of multiplying one number by another.							
Remainder – The amount left over after a division when the divisor is not a factor of the dividend.							
Scaling – Enlarging or reducing a number by a given amount, called the scale factor.							
Stage 1							
Solve 1-step problem	s using multiplication						
Example ques	tion: 5 x 4 = 20						



Concrete:	Pictorial:	Abstract:						
Hundreds Terms Disk	Hundreds Terms Draw	$34 \times 5 = 170$						
Hundreds Tens Ones	Hundreds Tens Ones	нто НТО						
		3 4 3 4						
		× 5						
		+ 1 5 0 (5 × 30) 1 7 0						
		1 7 0 1 2						
The place value and base 10 resources should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge. This should support their knowledge that multiplication is repeated addition. The place value and base 10 resources the understanding of the method rather than supporting the multiplication, as children should use times table knowledge. This should support their knowledge that multiplication is repeated addition. The place value and base 10 resources the understanding of the method rather than supporting the multiplication, as children should use times table knowledge. This should support their knowledge that multiplication is repeated addition. If the children do not, the quare given should reflect their knowledge. If the children do not, the quare given should reflect their knowledge. If the children do not, the quare given should reflect their knowledge. If the children do not, the quare given should reflect their knowledge. If the child only knows the 2, 5 tables, the 1-digit number should not their times tables, reaccognitive load.								
	Stage 3							
N	Iultiply 3-digit numbers by 1-digit numbe	rs						
Example question: 245 x 4 = 980								



Concrete: Image: State of the state o	Pictorial: ***********************************	Abstract: Th H T O 1 8 2 6 × - - - 5 4 7 8 2 1 - - 1,826 × 3 = 5,478 - - -				
When multiplying 4-digit numbers, place v use to support children in their understandi If the children are multiplying larger num encourage the use of multiplication grids written method.	If the children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so the children can focus on the use of the written method. When using the formal written method, the children need to ensure that they put the exchanged number at the bottom (as with addition). The children should not be using the expanded method at this point, unless absolutely necessary.					
Stage 5						
Λ	Aultiply 2-digit numbers by 2-digit numbe	rs				
Example question: 22 x 31 = 682						

Concrete:	20 2	Pictorial:	20 2	Abstract:					
<u></u>						н	Т	0	
				× 20 2			2	2	
				30 600 60	×		3	1	
			30-	1 20 2			0		
							2	2	
○ ○ ○ ○						6	6	0	
				$22 \times 31 = 682$	2	6	8	2	
When multiplying a multi-digit number by a 2-digit number, use the area model (using base 10) to help the children understand the size of the numbers thy are using. This links to finding the area of a rectangle by finding the space covered by the Base 10. This is an unusual method and teachers should ensure they understand and are comfortable using this method. Once the children are comfortable using the Base 10, they should then apply this knowledge to the place value counters. Place value counters are also easier for the children to draw into their books.									
	M	ultiply 3-digit numbe	ers by 2-digit numbe	rs					
		Example question	$: 234 \times 32 = 7,488$						

Image: Contract of the children can continue to use the area model when multiplying 3-digit by 2-digis. The children should be encouraged to move towards the formal written method						
Image: Second						
Image:						
1 1						
The children can continue to use the area model when multiplying 3-digit by 2-digis. Place value counters become more effective to use but Base 10 can be used to						
The children can continue to use the area model when multiplying 3-digit by 2-digis. Place value counters become more effective to use but Base 10 can be used to move towards the formal written method						
The children can continue to use the area model when multiplying 3-digit by 2-digis. Place value counters become more effective to use but Base 10 can be used to highlight the size of numbers, as with the previous stage. Any exchanges should be placed in box to the left; the next place vo column – as seen above.						
Stage 7						
Multiply 4-digit numbers by 2-digit numbers Example question: 2,739 x 28 = 76,692						

Concrete:	Abstract: 2,7	39	× 2	28 =	= 7(6,69	92
		TTh	Th	н	т	0	
			2	7	3	9	
		×			2	8	
Distanial		22	1 5	9 3	1 7	2	
Pictorial:		5 1	4	7 1	8	0	
		7	6	6	9	2	
	When multiplying 4-digitd I method. If they are still strugg focusing on the use of the m make this consistent.	by 2-c gling, j nethoc	digits, orovic J. Cor	child de mu nsider	ren st Itiplico where	nould ation (e exch	be confident in the written grids to support when they are nanged digits are placed and

Division

EYFS:	Year 1:	Year 2:	Year 3:	Year 4:	Year 5:	Year 6:
Doubling, sharing and grouping.	Solve one-step problems involving division by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.	Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs. Show that division is not commutative. Solve problems involving division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts.	Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. Solve problems, including missing number problems, involving division.	Recall division facts for multiplication tables up to 12 × 12. Divide mentally, including dividing by 1. Recognise and use factor pairs and commutativity. Solve problems involving multiplying two- digit numbers by one digit, integer.	Identify and understand multiples and factors; square numbers and cube numbers; prime numbers and composite numbers. Divide numbers up to 4 digits by a one- or two-digit number using a formal written method (short division), including long division for two-digit numbers – including remainders. Divide whole numbers by 10, 100 and 1000.	Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context. Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.

Key Vocabulary:	STEM Sentences:					
Array – An ordered collection of counters, cubes or other item in rows and columns.	'There are apples have been shared into groups. There are apples in each group.'					
Exchange – Change a number or expression for another of an equal value.	'There are groups of; there are altogether.'					
Factor – A number that multiplies with another to make product.	' is divided into groups of There are groups.'					
Partitioning – Splitting a number into its component parts.	' is divided into groups of'					
Quotient – The result of a division. Remainder – The amount left over after a division when the divisor is not a factor of the dividend	' is divided into groups of with a remainder of'					
Scaling – Enlarging or reducing a number by a given amount, called the scale factor.	' divided by ten is equal to'					
Stage 1						

Solve 1-step problems using multiplication (sharing)							
	Example question: 20 / 5 = 4						
<u>Concrete:</u>	Pictorial:	Abstract:					
		$20 \div 5 = 4$					
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	There are 20 apples altogether. They are shared equally between 5 bags. How many apples are in each bag?					
Children should solve problems by sharing concrete objects into equal groups. Sharing using concrete resources should be secure before moving to pictorial representations. In Year 1, children are not expected to record division formally; they are only expected to use concrete and pictorial representations. The children should not be introduced to the word division; they should only be using the word ' sharing' . In Year 2, children are introduced to the division symbol. The abstract should be shown alongside the concrete and/or pictorial representations.	Pictorial representations should only be used once the children understand the concept of sharing using concrete resources. A good transition from the pictorial understanding to the abstract is using bar models. They can start by dividing dots into the lower box on a bar model; then they can do the same activity using abstract numbers, as seen above.	The children should be introduced to the division symbol in Year 2. When this is first introduced, the abstract should be shown alongside the concrete and pictorial. The children need to see the relationship between the abstract symbol and the process of sharing.					
Stage 2							
So	lve 1-step problems using division (gr	ouping)					

Example question: 20 / 5 = 4						
Concrete:	Pictorial:	Abstract:				
		$20 \div 5 = 4$				
		There are 20 apples altogether. They are put in bags of 5.				
		How many bags are there?				
Children should solve problems by grouping the objects and then counting the number of groups. Grouping encourages children to count in multiples and links to repeated subtraction on a number line. They use concrete representations in fixed groups, such as, Numicon which helps to show the link between multiplication and division.	The pictorial should be use alongside the concrete. Initially, the children should be drawing the concrete resource they have been using. Bar models can also be used to support grouping as well – as seen above.	The children should be introduced to the division symbol in Year 2. When this is first introduced, the abstract should be shown alongside the concrete and pictorial. The children need to see the relationship between the abstract symbol and the process of grouping.				
Stage 3						
Divide 2-digit by 1-digit (sharing with exchange and remainders)						
Example question: 53 / 4 = 13r1						

Concrete:	<u>Pictorial:</u>	Abstract:				
Tens Ones 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Tens Ones Tens Ones 10	$52 \div 4 = 13$ 1 3 4 5 12				
When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor. Language is important here. Children should consider, 'How many groups of 4 tens can we make?' and, 'How many groups of 4 ones can we make?' Remainders can also be seen as they are left ungrouped. While the children are learning about the concrete, they should also have the abstract visible. The abstract should not be explained but it should be visible.	When the children are first introduced to the abstract representation, they should have the concrete and pictorial resources visible as well. They need to see the link between what they have been doing with the concrete/pictorial and how that is represented through the abstract.					
Stage 5						
Divide 3-digit by 1-digit (grouping)						
Example question: 856 / 4 = 214						

Concrete:	Pictorial:	Abstract:					
Hundreds Tens Ones Oracle Ora	Hundreds Tens Ones Hundreds Tens Ones	$856 \div 4 = 214$ $4 8 5 16$					
Children should continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number. Place value counters or plain counters can be used on the place value grid to support this understanding.	When pictorial representations are first used, they should be used in conjunction with the concrete resources. This should ensure that the understanding from using the concrete resources transfers to the pictorial representations. When moving to the pictorial, the children should be able to draw out their place value grid and fill in the counters, ensuring the draw around the groups.	The abstract should be shown alongside the concrete and pictorial. This is to ensure that they understand what is happening when they are using the abstract.					
Stage 6							
Divide 4-digit by 1-digit (grouping)							
	Example question: 8,532 / 2 = 4,26	6					
<u>Concrete:</u>	Pictorial:	Abstract:					

		8,532 ÷ 2 = 4,266 4 2 6 6 2 8 5 $^{1}3$ $^{1}2$						
Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1- digit numbers. Children can also draw their own counters and group them through a more pictorial method. Children should be encouraged to move away from the concrete and pictorial representations when dividing numbers with multiple exchanges.	The children should be able to represent what they have done in pictorial form. The easiest way to do this is to use place value counters for both.	The children should be using the abstract more when more exchanges occur. When they children are being taught this process, the teacher should model to them how to check their work for mistakes. At this stage, when using the formal written method, short division, the children need to ensure they place the exchanged number in the top left-hand side of the box to the right.						
Stage 7								
Divide any number by 2-digit numbers (short division) Example question: 432 / 12 = 36								

Concrete:	Abstra	act:									
			0	3	6	(
		12	4	4 3	7 2		432	2 ÷ '	12 =	36	J
							0	4	0	0	
	7.3	35 ÷	- 15 =	= 48	9		0	7_	13_	9 13_	
Pictorial:						15	7	3	3	5	
	15	30	45	60	75	90	105	120	135	150	
	When children begin to divide up to 4-digits by 2 digits, the written methods become the most accurate as concrete and pictorial representations become less effective. Children can write our multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient (a result obtained by dividing one quantity by another) can be rounded as appropriate. At this stage, when using the formal written method, short division, the children need										
	to ensui the righ	re they p t.	blace th	e excho	anged n	umber in	the top	left-har	nd side	of the b	ox to
Stage 8											
Divide any number by 2-digit numbers (long division) Example question: 432 / 12 = 36											

<u>Concrete:</u>	Abstract: 0 3 6 12×1=12 1 2 4 3 2 12×3=36 12×4=48 - 3 6 0 12×5=60 12×5=60 - 7 2 - 7 2 12×6=72 - 7 7 2 12×7=84 12×7=108 12×7=108 12×1=12 12×1=12 12×1=12 12×2=24 12×1=12 12×3=36 12×5=60 12×5=60 12×7=108 12×7=108 12×10=120 120				
Pictorial:	7,335 ÷ 15 = 489 $1 \times 15 = 15$ $2 \times 15 = 30$ $3 \times 15 = 45$ $- 1 2 0 0$ $- 1 3 5$ $- 1 2 0 0$ $- 1 2 0 0$ $- 1 3 5$ $- 1 2 0 0$ $- 1 2 0 0 0$ $-$				
Stage 9					
Divide any number by 2-digit numbers (long division with remainders) Example question: 372 / 15 = 24r12					

Concrete:		Abstract:			1			_		
					_	2	4 r	1	2	1 × 15 = 15
				1	5 3	7	2			2 × 15 = 30
		7	70 . 15 04 . 10		- 3	0	0			$3 \times 15 = 45$
		3	$72 \div 15 = 24 r 12$			7	2			$4 \times 15 = 60$
					-	6	0			5 × 15 = 75
						1	2	-		$10 \times 15 = 150$
			Com	olete	the n	umbe	er trac	k wi	ith the	multiples of 15
			1 5 3 7 2	(
Pictorial:			- 3 0 0		37	2 ÷	- 15	=	$24\frac{2}{2}$	
			7 2	l					:)
			- 6 0							
			1 2							
		When a remaind	ter is left at the end of	a ca	alcu	latio	on. d	chil	dren	can either leave it as a
		remainder or col	nvert it to a fraction. Th	nis w	rill d	epe	end	on	the c	context of the question.
		They can also an	nswer questions where t	he c	lnot	ient	nee	eds	to be	e rounded according to
		the context. The	children should also w	rite	out	the	nur	mb	er tro	ack for the multiple that
		they are dividing	g by. They can write it a	out ł	now	eve	er th	ey	like b	out it should be there to
		avoid mistakes.								
		Fr	actions							
EYFS: Year 1: Year	2: Year	3: \	Year 4:	Ye	ar	5:				Year 6:

	Recognise, find and name a half as one of two equal parts of an object, shape or quantity. Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.	Recognise, find, name and write fractions 1/3 , 1/4 , 2/4 and 3/4 of a length, shape, set of objects or quantity. Write simple fractions for example, 1/2 of 6 = 3 and recognise the equivalence of 2/4 and 1/2.	Count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one- digit numbers or quantities by 10. Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators. Recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators. Recognise and show, using diagrams, equivalent fractions with small denominators. Add and subtract fractions with the same denominator within one whole [for example, 5/7 + 1/7 = 6/7]. Compare and order unit fractions, and fractions with the same denominators.	Recognise and show, using diagrams, families of common equivalent fractions. Count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten. Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number. Add and subtract fractions with the same denominator Solve simple measure and money problems involving fractions and decimals to two decimal places.	Compare and order fractions whose denominators are all multiples of the same number. Identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, 2/5 + $4/5 = 6/5 = 1 1/5$]. Add and subtract fractions with the same denominator and denominators that are multiples of the same number. Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.	Use common factors to simplify fractions; use common multiples to express fractions in the same denomination. Compare and order fractions, including fractions > 1. Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions. Multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $1/4 \times 1/2 = 1/8$]. Divide proper fractions by whole numbers [for example, $1/3 \div 2 = 1/6$].
--	--	---	---	--	---	--

Key Vocabulary:	STEM Sentences:

Numerator – the top digit of a fraction.	'The whole has been divided into equal parts and we				
Denominator – the bottom digit of a fraction.	have parts. This represents [?] / _? .'				
Proper Fractions – fractions that are less than 1.	'I have folded my whole length of paper into equal/unequal parts.'				
Improper Fractions – fractions that are more than 1.	'The parts are equal/unequal. I know this because the				
Mixed Number – a mixed number is a combination of a	number of in each part is the same.'				
whole number and a proper fraction that is less than 1.	'If is the whole, then is part of the whole.'				
Equivalent – the same value.	'The denominator is because the whole is divided into				
Simplifying – dividing the digits in the fractions to their	equal parts.'				
"smallest" form by using a common factor.	'There are parts between zero and one. This means				
Compare – ordering or looking at the different values of	we are counting in units of'				
tractions.	'Each interval on the line is divided into equal parts. This				
Integer – a whole number.	allows us to count in				
Unit Fractions – fractions where the numerator is 1.					
Non-unit Fractions – fractions where the numerator is					
greater than 1.					
Stage 1					
Recognise and understand the value of simple fractions					
Example: $\frac{1}{2} \frac{1}{3} \frac{1}{4} \frac{2}{4} \frac{3}{4}$					

immediately. The understanding here should be about something being part of a whole. Start big (Europe) and then 'zoom in' (e.g. UK, streets, animals then counters). If the children have a deep understanding of this concept, then they will have a better understanding of fractions as a whole later. This stage comes before the children move on to other fractions. It is important to use linear models at this early stage because, at later stages, children will need to understand fractions as numbers that can be positioned on a number line. Children can also cut out shapes and cut them into equal/unequal parts.

Most of the concrete resources can also be represented as pictorial representations. Using pictorial representations that match the concrete resources will help the children transfer their understanding. One might be shapes. The children can divide shapes in to equal/unequal parts. Focus should be on the term 'equal parts'. Children do not need to use the word 'congruent' at this stage but should understand the concept of the parts looking the same. The children need to be exposed to object that are the same but have been divided into unequal groups. E.g. 3 squares that have all been divided into 4 part but in different ways – as seen above.

Stage 3 Identifying, representing and comparing unit fractions Example question: $\frac{1}{3} > \frac{1}{4} > \frac{1}{10} > \frac{1}{1000}$

Concrete:	Pictorial:	Abstract:
$\frac{1}{3} \text{ full} \qquad \frac{1}{4} \text{ full} \qquad \frac{1}{10} \text{ full} \qquad \frac{1}{1000} \text{ full}$		$\frac{1}{3} > \frac{1}{4} > \frac{1}{10} > \frac{1}{1000}$
At this stage, the children should be looking at the same model alongside each other and explore how the same whole can be divided into different numbers of equal parts. 'What's the same, what's different?' It should be made clear to the children that a 'whole' can be whatever we define it. The children should also be exposed to situations and activities where the parts do not look the same, but the quantity within each part is equal. The children in the class could be the concrete resource, the class being the whole and the children being the parts.	Give the children plenty of practice looking at shapes, lines and sets, and identifying how many equal parts each is divided into. Make sure that the language used in the previous stages is also used here (part, whole, equal parts, numerator, denominator, etc.).	The children should be taught to write fractions using the 'bar first' method. This is where the children draw the division bar first before writing in the digits. They should be drawing the bar, then the denominator and then the numerator. This supports children's understanding of a fraction being part of a whole that has been divided. When working in the abstract at this stage, the children need to understand, 'when the numerator is the same, the larger the denominator the smaller the fraction'.
Stage 4		
Identifying, representing and comparing non-unit fractionsExample question: $\frac{4}{7} > \frac{3}{7} > \frac{2}{7}$		

Concrete:	Pictorial:	Abstract:	
$\frac{1}{10} \text{ m } \frac{1}{10} $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\frac{4}{6} \text{ is four lots of } \frac{1}{6}$ $\frac{4}{5} \text{ is four lots of } \frac{1}{5}$ I know that $\frac{1}{6} \text{ is less than } \frac{1}{5}$ So, four lots of $\frac{1}{6}$ is less than four lots of $\frac{1}{5}$ $\frac{1}{4} \text{ is one lot of } \frac{1}{4}$ $\frac{3}{4} \text{ is three lots of } \frac{1}{4}$ I know that 1 is less than 3, so $\frac{1}{4}$ is less than $\frac{3}{4}$	
Non-unit fractions are introduced through their connection to unit fractions. They are simply 'multiples' of unit fractions. These connections need to be made early on to support their understanding of non-unit fractions. While non-unit fractions are first being introduced, the language 'five one-sixths' should be used in the place of five sixths. Meter sticks are a good concrete resource to use to demonstrate tens. Concrete representations should allow children to explore fractions of a whole and what it means to have more than one part of it – non unit fractions.	When the meter ruler is used as a concrete resource, it can easily be transferred into pictorial bar models. The children should be exposed to area models, linear models and as quantities. When using pictorial resources, it should be clear whether the parts are equal or unequal parts.	As in the previous stage, the children should be using the 'bar first' method for writing fractions. The abstract should still be being used alongside the concrete and pictorial as this will help children understand the concept of non-unit fractions. When working in the abstract at this stage, the children need to understand, 'when the denominator is the same, the smaller the numerator the smaller the fraction'.	
Stage 5			
Adding and subtracting fractions within one whole			
Example question: $\frac{3}{9} + \frac{4}{9} = \frac{7}{9}$ and $\frac{8}{9} + \frac{3}{9} = \frac{5}{9}$			

Concrete:	Pictorial:	Abstract:	$\frac{8}{-}$ is 8 lots of $\frac{1}{-}$	
$\frac{7}{10} - \frac{3}{10} = \frac{4}{10}$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\frac{3}{9} \text{ is } 3 \text{ lots of } \frac{1}{9}$ $\frac{4}{9} \text{ is } 4 \text{ lots of } \frac{1}{9}$ $\text{I know that } 3 + 4 = 7$ So I know that $\frac{3}{9} + \frac{4}{9} = \frac{7}{9}$	$\frac{3}{9} \text{ is 3 lots of } \frac{1}{9}$ $\frac{3}{9} \text{ is 3 lots of } \frac{1}{9}$ $8 - 3 = 5$ $80 \frac{8}{9} - \frac{3}{9} \text{ is } \frac{5}{9}$	
At this stage, it is important that the children understand that non-unit fractions are the repeated addition of unit fractions. This helps them to not add or subtract the denominators when adding and subtracting fractions. Alongside concrete resources, using stories and real-life situations should be used to support the children's understanding of fractions. For example, Jack eats three nineths of a pizza, Beth eats two nineths of a pizza. How much pizza did they eat altogether.	Pictorial representations should be used heavily at this stage. They should be used both as questions and as a way for children to explain their reasoning. Again, stories and real-life problems are key to the children's understanding of adding and subtracting fractions. Number lines and bar models are one of the most beneficial pictorial representations that can be used. Generaliser – 'When adding or subtracting fractions with the same denominators, just add or subtract the numerators.'	At this stage the written be left until later in the lessons. This is the here children from slipp misconceptions that add/subtract the denore the numerator. Once understand adding of fractions with the same they should also be to inverse and how it works as whole numbers. $3 + 4 = 7 \qquad 7 - 4 = 3$ $\frac{3}{10} + \frac{4}{10} = \frac{7}{10} \qquad \frac{7}{10} - \frac{4}{10} = \frac{7}{10}$	abstract should be sequence of elp prevent the ing into the they need to ninator as well as the children and subtracting be denominator, aught about the in the same way $\frac{3}{10}$	
Stage 6				
Improper and mixed number fractions – crossing the whole				
Example question: $\frac{7}{5} + \frac{3}{5} = \frac{10}{5} = 2$				

Concrete:	Pictorial:	$\frac{7}{5} + \frac{3}{5}$	Abstr	act:	
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\frac{1}{10}$ $\frac{21}{10}$ $3\frac{3}{5}$ $3 + 2$ $3 + 2$	Prompt question How many groups of $\frac{10}{10}$ in $\frac{21}{10}$? (2 groups and 1 more tenth.) + $2\frac{4}{5}$ 2 $\frac{4}{5}$ 2 $\frac{4}{5}$ 2 $\frac{4}{5}$ 2 $\frac{4}{5}$ 20 $\frac{8}{10}$ - $12\frac{2}{7}$ 12 $-2\frac{12}{7}$ 5 $\frac{7}{5}$ $18\frac{3}{20}$	Mixed number $2\frac{1}{10}$ ion calculations: $\frac{6}{9} + 5$ $\frac{1}{15} + 7$ $5\frac{1}{8} - \frac{1}{8} =$ $= 3 - \frac{1}{4}$
This will be the first time that the children experience fractions crossing the whole. They will do this initially through mixed number fractions and then move on to improper fractions. Concrete manipulatives are critical in ensuring the pictorial area models can be understood and accessed by all; fraction tiles can be useful for this.	The area mode be mostly in a model) or in a chart). It is in exposed to bo easier for child clearly show w a whole. Num alongside area The part-part- encouraging c previous additio	els used at this stage should linear form (similar to a bar circular form (similar to a pie nportant that children are th forms. The linear model is dren to draw but does not then fractional parts exceed aber lines should be shown models as often as possible. whole model is useful for children to connect back to on and subtraction.	When i should have adden the firs good questic contex	moving into the abstra be exposed to questic the whole number d and some with the t addend. Units of me way of presenting ons to the children to and support understa	act, children ins that both as the first fraction as asure are a g abstract give them anding.
Stage 7					
	Multiplying wh	ole numbers and fractions			
	Example quest	ion: $\frac{1}{8} \times 4 = \frac{4}{8}$ or $\frac{4}{5} \times 3 = \frac{12}{5} = 2\frac{2}{5}$			

Concrete:	Pictorial: $1 + \frac{4}{5} + \frac{4}{5} + \frac{4}{5} + \frac{4}{5}$	$ \underline{Abstract:} \qquad \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} \\ $	
When children are first introduced to this concept, the teacher should clearly reference multiplication of whole number that they have learnt previously. This means that is should be presented to them as repeated addition – as seen previously in the multiplication section. Concrete resources should be used alongside the pictorial and abstract resources.	Number lines are one of the key pictorial resources when representing repeated addition. They are also useful for showing when multiplying they will often cross the whole. Area models, number lines and bar models should be used heavily at this stage.	When working in the abstract, the children will either continue to use repeated addition or work with scaling – finding the value of the unit fraction and then multiplying it by the number of them you need (the numerator). E.g. $\frac{2}{3} \times 60$. If $\frac{1}{3}$ of 60 is 20 then $\frac{2}{3}$ of 60 is 40.	
Stage 8			
Finding equivalent fractions and simplifying fractions			
Example question: $\frac{1}{4} = \frac{3}{12}$			

Concrete:	Pictorial:	Abstract:	
1 1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\frac{4}{12} + \frac{1}{12} = \frac{5}{12} \frac{1}{3} + \frac{1}{12} = \frac{5}{12} \frac{4}{13} = \frac{4}{13}$ $\frac{3}{9} + \frac{1}{9} = \frac{4}{9} \frac{1}{3} + \frac{1}{9} = \frac{4}{9}$ Try to balance the move to more efficient procedures with sense-checking their calculations. For example, $\frac{1}{3} + \frac{1}{4}$ can't be $\frac{1}{7}$ because $\frac{1}{7}$ is smaller than both the addends. When working in the abstract, if the children are not secure in their times tables, ensure that they have a times table grid next to them.	
Stage 10			
Multiplying fractions and dividing fractions by a whole number			
Example question:			

<u>Concrete:</u>	Pictorial:	Abstract:	
1 one 1 tenth 1 hundredth	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\frac{4}{5} \times \frac{2}{3} = \frac{8}{15} \qquad \frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$ $\frac{8}{11} \div 2 = \frac{4}{11}$ $\frac{9}{12} \div \frac{5}{12} = \frac{9}{12} \times \frac{1}{5} = \frac{9}{60}$	
A fundamental concept is that multiplying a number by a proper fraction makes it smaller. This conceptual understanding is just as important as being able to perform a procedure for multiplying and dividing fractions. The idea that when we multiply by a proper fraction, we are making a number smaller, is really significant because in some branches of higher mathematics, division ceases to be a concept that is used, since any division can be replaced by multiplication. For example, dividing by 4 becomes multiplying by $\frac{1}{4}$.	As the procedures for multiplying pairs of fractions and dividing fractions by whole numbers are so simple children may become fluent quickly. Initially, if the children have picked up the procedure quickly, they should be able to draw diagrams to explain the process.	If is useful for children to simplify fractions before completing these types of calculations. The children should also be using their sense-checking – making sure the answer is smaller than the number in the question. This demonstrates their deeper understanding. Questions should be written with the multiplier and multiplicand in either position. E.g. three lots of $\frac{1}{5}$ can be written as $3 \times \frac{1}{5}$ or $\frac{1}{5} \times 3$ or $\frac{1}{5}$ of 3. With division, it would be $\frac{1}{2} \times \frac{1}{3}$ or $\frac{1}{2} \div$ 3.	
Stage 11			
Linking fractions, decimals and percentages			
Example question:			

